

# Parallel Modeling of Three-Dimensional Scramjet Combustor and Comparisons with Experiment's Results

Zheng Zhong-hua    Le Jia-ling

(China Aerodynamics Research & Development Center, Mianyang 621000, China)

## Abstract

In this paper a parallel simulation of an experimental dual-mode scramjet combustor configuration is presented. Turbulence is modeled with the  $\kappa$ - $\varepsilon$  two-equation turbulence model and a 7-species, 8-equation kinetics model is used to model hydrogen/air combustion. The conservation form of the Navier-Stokes equations with finite-rate chemistry reactions is solved using a diagonal implicit finite-volume method. Using about 3,120,000 grid points, the three-dimension flow-fields with equivalence ratio  $\phi=0.0$  and 0.35 have been respectively simulated on the parallel computer system, obtaining more detailed flow properties than the experiment's results. Wall pressure comparisons between CFD and experiment show fair agreement. For  $\phi=0.35$ , the fuel-penetrating height of the seven injectors are different because of the effects of the boundary layer and the shock wave in the combustor. According to numerical results, if adjusting the locations of the injectors, the combustion efficiency could be improved.

## Introduction

Supersonic combustion ramjet engine (Scramjet), in which the combustion process can be supersonic, is a new type of air-breathing propulsion device. It has remarkable performance, great potential superiority, and a good prospect in the field of military and civil aviation in the future. However, the experimental study of scramjet engine puts higher demands on simulating capability of ground test facilities, and greatly increases the test cost and period. Since the flow residence time within a combustor is very short, on the order of one millisecond, it is difficult to measure the flow-fields, generally only get the wall pressure and heat flux. Even using advanced measure technology(Planar Laser Induced Fluorescence), which is expensive, it's still difficult to make three-dimensional measurements, hence difficult to obtain detailed flow properties. With the development of computer technology and the advancement of numerical calculation, Computational Fluid Dynamics (CFD) can provide detailed flow-field characteristics than experimental results and has emerged as an extremely valuable and cost-effective engineering tool in combustor's design and analysis.

Previous work in the area of combustor analysis and predictive capability includes the early work of Billing<sup>1</sup>, Billing et al<sup>2</sup>, and Waltrup and Billing<sup>3,4</sup>. They developed correlations based on one-dimensional and two-dimensional flow analysis which included such drivers as incoming boundary-layer thickness and maximum combustor pressure rise. These correlations perform well on simple model geometries (axi-symmetric or two-dimensional) but are not generally suitable for more complex three-dimensional problems except for providing directions and trends. Recent computational studies of the three-dimensional combustors are described in papers by Rodriguez et al<sup>5</sup> and Riggins<sup>6</sup>. The computational domains include the use of jet-to-jet symmetry and entire half-duct modeling. Calculations in each case are typically conducted on fixed structured grids of

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less than 2,500,000 points in multi-zone domains. Among all the numerical simulations the fuel-penetrating heights of different injectors have not been obtained.

This paper is intended to provide a parallel simulation of an experimental dual-mode scramjet combustor configuration. The full duct for the isolator-combustor is then modeled in order to study the fuel-penetrating height of the seven injectors. The grid used for the present calculations is  $211 \times 41 \times 121$  for the isolator and  $211 \times 81 \times 121$  for the combustor, about 3,120,000 grid points. Using the Navier-Stokes equations with the addition of conservation of chemical species, the three-dimension flow-fields with equivalence ratio  $\phi=0.0$  and  $0.35$  have been respectively simulated on the parallel computer system, obtaining more detailed flow properties than the experiment's results. Wall pressure comparisons between CFD and experiment show fair agreement.

### Governing Equations and Numerical Method

In general curvilinear coordinate, the full, three-dimensional Navier-Stokes equations coupled with chemical nonequilibrium processes in a nondimensionalized conservation form are written as

$$\frac{\partial U}{\partial t} + \frac{\partial E}{\partial \xi} + \frac{\partial F}{\partial \eta} + \frac{\partial G}{\partial \zeta} = \frac{1}{R_e} \left( \frac{\partial E_v}{\partial \xi} + \frac{\partial F_v}{\partial \eta} + \frac{\partial G_v}{\partial \zeta} \right) + S$$

where U are the conservation variables, E、F and G are the convective fluxes,  $E_v$ 、 $F_v$  and  $G_v$  are the viscous fluxes, and S are the production and reduction rates for the nonequilibrium processes.

The conservative form of the equations is solved using a diagonal implicit finite-volume method, which approximately solves this system using two sweeps of a point Gauss-Seidel relaxation. In the explicit part, the inviscid fluxes are computed using Steger-Warming scheme with a 3rd-order accurate MUSCL interpolation. The viscous fluxes are evaluated using standard central differences. For the implicit calculation, the code uses a diagonal algorithm, which eliminates the expense of inverting large block matrices that arise in chemically reacting flows.

The first step:

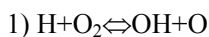
$$\left[ \mathbf{1} + \Delta t (\lambda_{A\max} + \lambda_{B\max} + \lambda_{C\max}) - \Delta t D \right] \overline{\delta U^{n+1}} - \Delta t \left( A_{i-1}^+ \delta U_{i-1}^n + B_{j-1}^+ \delta U_{j-1}^n + C_{k-1}^+ \delta U_{k-1}^n \right) = \Delta t RHS$$

The second step:

$$\left[ \mathbf{1} + \Delta t (\lambda_{A\max} + \lambda_{B\max} + \lambda_{C\max}) \right] \delta U^{n+1} + \Delta t \left( A_{i+1}^- \delta U_{i+1}^n + B_{j+1}^- \delta U_{j+1}^n + C_{k+1}^- \delta U_{k+1}^n \right) = \left[ \mathbf{1} + \Delta t (\lambda_{A\max} + \lambda_{B\max} + \lambda_{C\max}) \right] \overline{\delta U^{n+1}}$$

### The Chemical Reacting Model

A combustion model for hydrogen/air<sup>7</sup> mixtures consisting of 8 reactions and 7 species, including 6 reacting species  $H_2$ 、 $H_2O$ 、 $O$ 、 $H$ 、 $OH$ 、 $O_2$  and an inert specie  $N_2$ , is selected for our computations. The eight reactions are:



- 2)  $O+H_2 \rightleftharpoons OH+H$
- 3)  $H_2+OH \rightleftharpoons H+H_2O$
- 4)  $2OH \rightleftharpoons O+H_2O$
- 5)  $H_2+M_1 \rightleftharpoons 2H+M_1$
- 6)  $H_2O+M_2 \rightleftharpoons OH+H+M_2$
- 7)  $OH+M_3 \rightleftharpoons O+H+M_3$
- 8)  $O_2+M_4 \rightleftharpoons 2O+M_4$

The reaction rates are taken from Evans and Schexnayder<sup>8</sup>.

### Boundary Condition

The free-stream is supersonic so that all flow variables are known. Exit conditions are set as supersonic extrapolation. The solid wall boundaries are modeled as no-slip, adiabatic, a zero normal gradient of pressure and fully non-catalytic.

## Results and Analysis

### 1. Code Validation

Shock induced combustion phenomena, ranging from decoupled to coupled shock-deflagration systems, were experimentally investigated in the mid 1960's and early 1970's. Calculations of this type of reaction are very demanding in terms of numerical robustness and accuracy, since the reactions usually occur very fast with significant energy release which takes place in a very short distance. In this paper, to validate the code, two results from Lehr's<sup>9</sup> experiment are reproduced numerically. The two cases are

Case	Mixture	$V_\infty$ (m/s)	$P_\infty$ (Pa)	$T_\infty$ (K)
1	H <sub>2</sub> /Air	2605	42662	250
2	H <sub>2</sub> /Air	1685	42662	250

All cases involve a sphere having a diameter of 15mm moving through a stoichiometric mixture at velocity, pressure and temperature indicated at the above table. Calculations are performed on a 45×80×41 grid.

Experimentally, Lehr found that Case 1 resulted in a coupled shock-deflagration system, whereas Case 2 resulted in a decoupled shock-deflagration system. The temperature contours of Case 1 along with the experimental shock location are shown in figure 1. Case 2 is a condition where a projectile is traveling at a speed lower than the detonation speed of H<sub>2</sub>/Air. This case resulted in a decoupled shock-deflagration system shown in figure 2. These two calculations correctly predict the location and the shape of the wave. So the code is right and reliable.

### 2. Description of the experiment

This section briefly describes the experimental configuration examined in this investigation. The scramjet is essentially a rectangular-section, constant-width duct. On both upper and lower walls there is a backward facing step and, further downstream, a 3° wall expansion only on the upper wall. These two features divide the scramjet into three sections: isolator, combustor and expansion. The steps have a height of 3mm. Injection takes place 95mm downstream of the steps. There are seven injectors on the bottom wall and the diameter of each injector is 1.2mm. Hydrogen is injected through the orifices at sonic conditions, with equivalence ratio  $\Phi=0.35$ . Other dimensions can be obtained from figure 3. For convenience, the nominal inlet conditions of the vitiated flow are provided in table 1. Table 2 gives the injectant conditions. This experiment

has been performed at CARDC.

**Table 1: Nominal inlet conditions.**

<b>M</b>	2.05	<b>P<sub>H2O</sub></b>	0.258
<b>P</b>	0.341Mpa	<b>P<sub>O2</sub></b>	0.21
<b>T</b>	1172K	<b>P<sub>N2</sub></b>	0.532
<b>U</b>	1417(m/s)		

**Table 2: Injectant conditions**

<b>M</b>	1.0	<b>P<sub>H2</sub></b>	1.0
<b>Pt</b>	2.3Mpa	<b>D</b>	1.2mm
<b>Tt</b>	300K	<b>Φ</b>	0.35

### 3. Results and Analysis

#### 1) $\Phi=0.0$

Without injection the wall pressures at the bottom on the center-plane are compared in figure 4 with the data of CARDC's experiment. The results show fair agreement.

#### 2) $\Phi=0.35$

For  $\Phi=0.35$ , figure 5 shows the wall pressure comparisons at the bottom on the center-plane. The peak pressure is almost equal and the results show also good agreement. Figure 6 gives the center-plane mach number floods. For this low- $\Phi$  condition the whole core flow is supersonic. Figure 7 shows the wall pressure comparisons of the numerical simulations between  $\Phi=0.0$  and  $\Phi=0.35$ . For  $\Phi=0.35$ , there is no upstream interaction and the combustion reactions only affect the downstream flow-field. In order to study the fuel-penetrating height of the seven orifices, the hydrogen-specie flood, the temperature flood and the pressure flood of the cross-section at the center location of the orifices are shown in figure 8. The hydrogen-specie flood shows the fuel-penetrating heights of the seven injectors are different. The temperature flood indicates that the fuel-penetrating height of the two side orifices is low for the impact of the side boundary-layer. At the same time, because of the suppressing of the shock plane, the penetrating heights of the three middle orifices are also low. According to numerical results, if adjusting the locations of the injectors, the combustion efficiency could be improved

### Conclusions

1. Wall pressure comparisons between CFD and experiment show fair agreement. So the code can be used for studying the data of experiments and getting more detailed properties of the experimental flow field.
2. Because of the effects of the boundary layer and the shock wave in the combustor, for  $\phi=0.35$ , the fuel-penetrating height is low and the combustion efficiency is low. Adjusting the locations of the injectors could improve the combustion efficiency.
3. For  $\Phi=0.35$ , the whole core flow is supersonic without upstream interaction. The combustion reactions only affect the downstream flow-field.

### Future Work

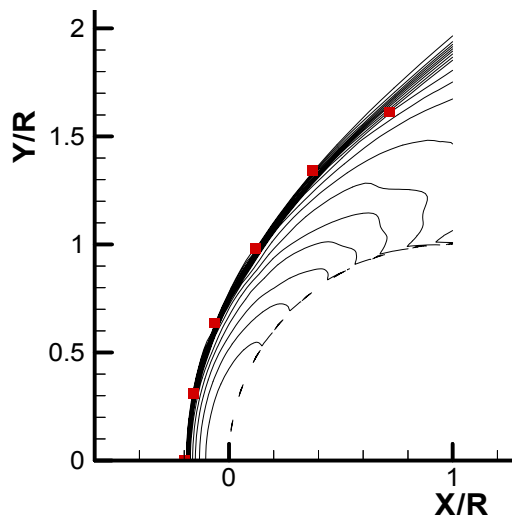
1. Unsteady analysis may be used for understanding the physics of fuel air mixing and for combustion instabilities.
2. Consider the turbulence-chemistry interactions.
3. More complex reaction mechanisms for hydrogen/air combustion will be needed, particularly

for hydrocarbon fuel.

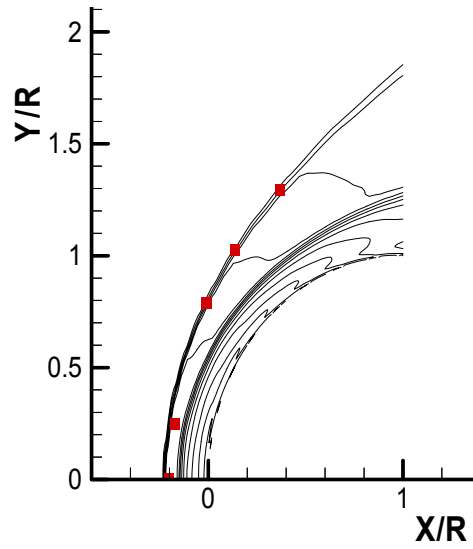
4. Increase the convergence rates of the code.

## Reference

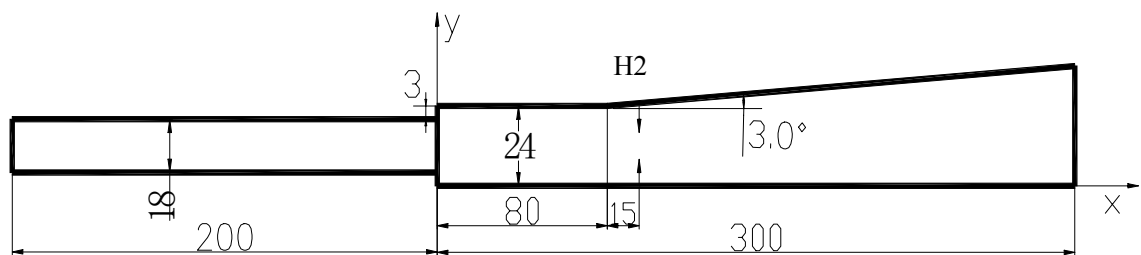
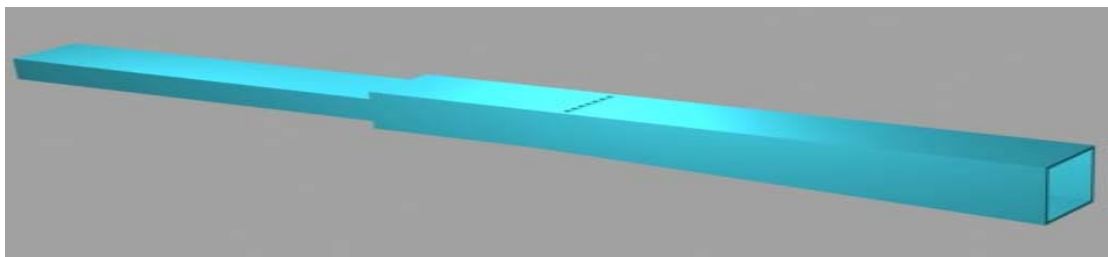
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**Figure 1: Coupled shock-deflagration system; Temperature contours**

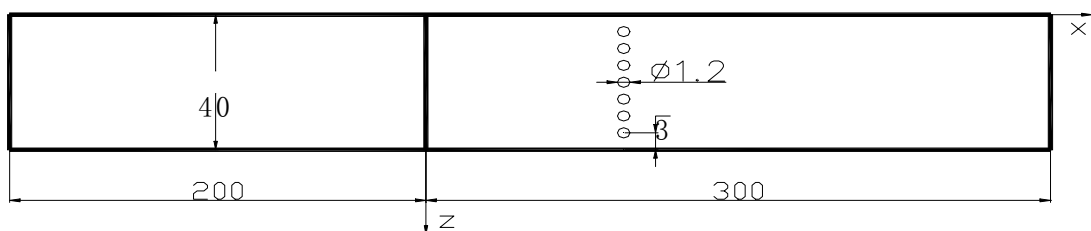


**Figure 2: Decoupled shock-deflagration system; Temperature contours**

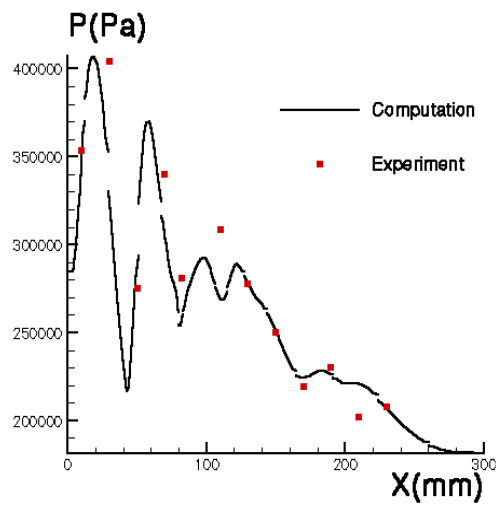


**Isolator**

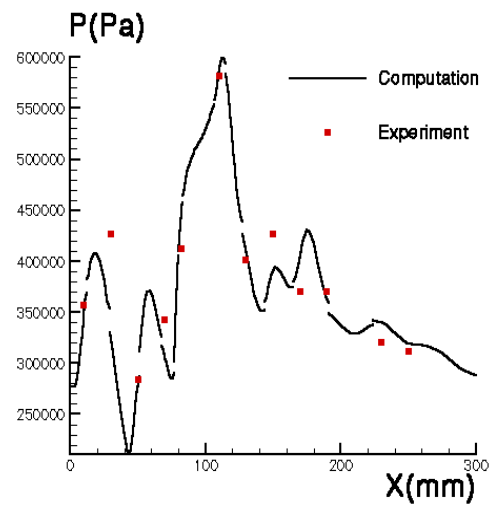
**Combustor**



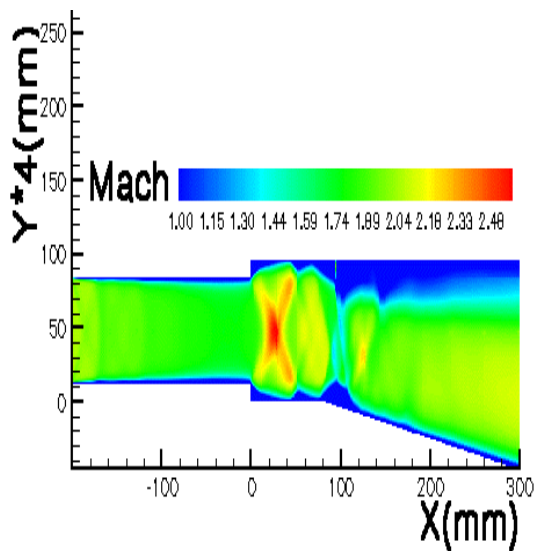
**Figure 3: Outline of the dual-mode scramjet experiment**



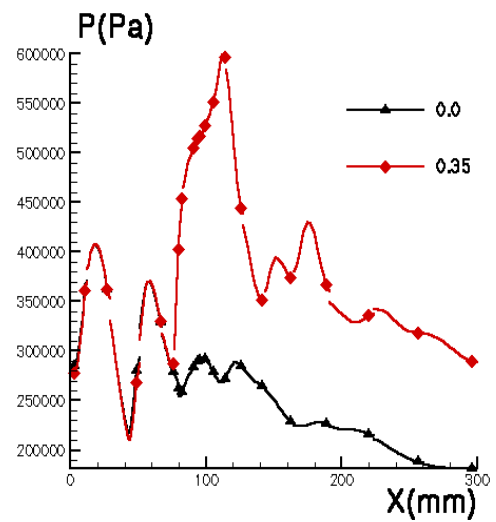
**Figure 4: Wall pressure comparisons for  $\Phi=0.0$**



**Figure 5: Wall pressure comparisons for  $\Phi=0.35$**

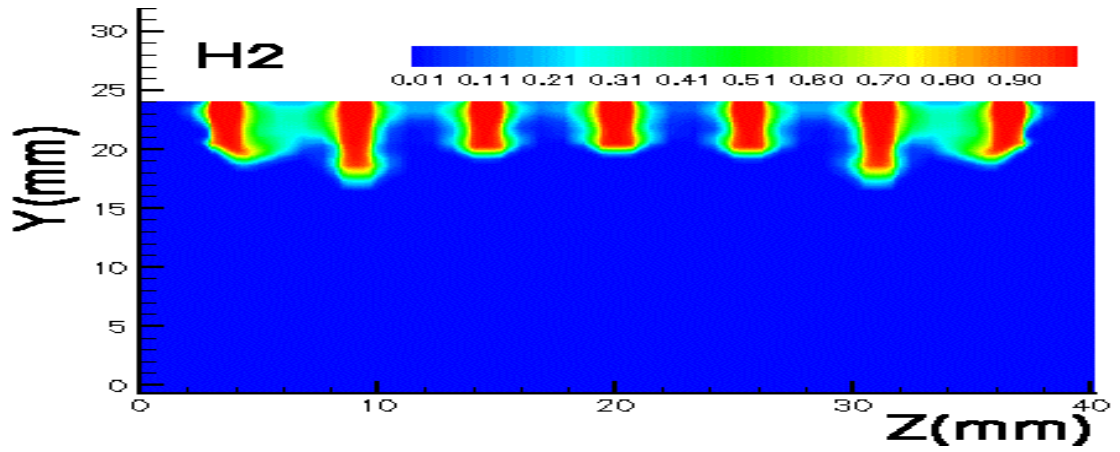


**Figure 6: Mach number floods of the centerplane for  $\Phi=0.35$**

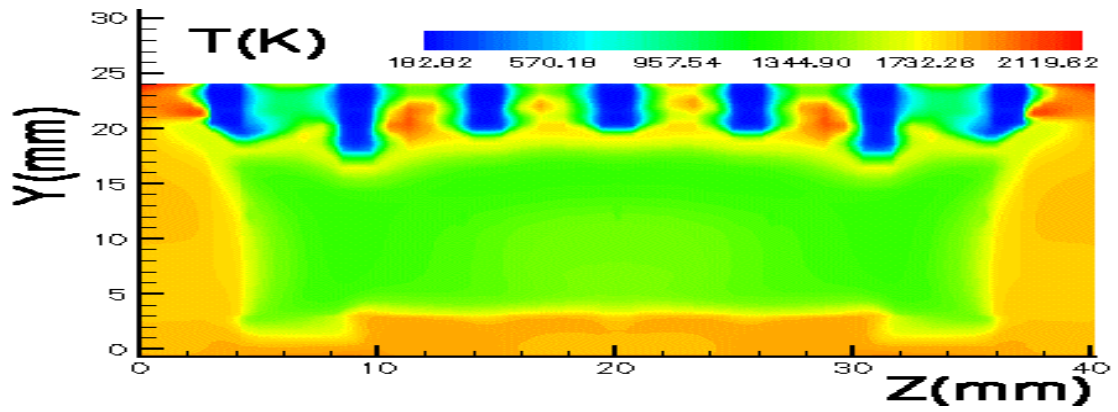


**Figure 7: Wall pressure comparisons between  $\Phi=0.0$  and  $\Phi=0.35$**

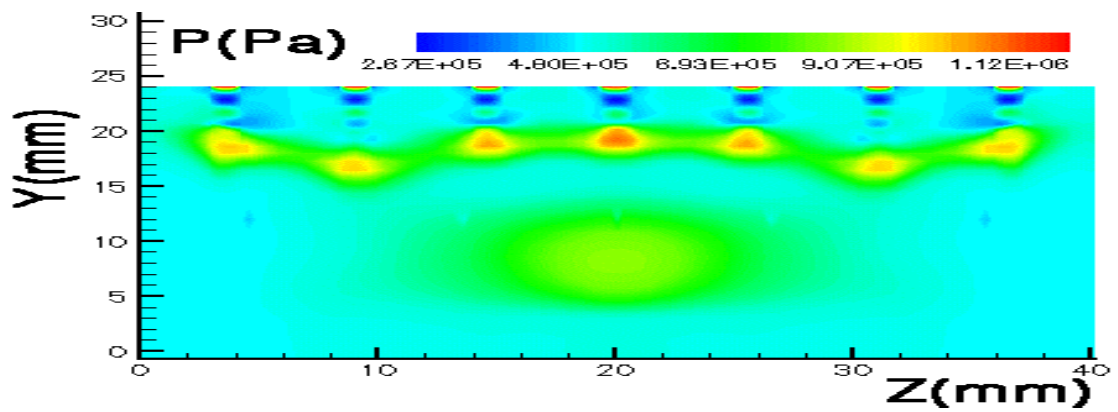




(a) Hydrogen-specie flood of the cross-section for  $\Phi=0.35$



(b) Temperature flood of the cross-section for  $\Phi=0.35$



(c) Pressure flood of the cross-section for  $\Phi=0.35$

Figure 8: Comparisons of the fuel-penetrating height of seven orifices